Math Rules Cyberspace

Travis H.

Stanford University, 16-17 Apr 2011



• Play clip 1 Cryptografie, Cryptografia intro clip (2:18)

Travis H. Math Rules Cyberspace

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Cryptology Shift Ciphers Substitution Ciphers Advanced Material Web Sites Hackers System Crackers Security Experts Cryptologists

Web Sites Castles on the Internet



- Have a practical purpose so can never be perfect
- More valuable the data, the stronger it must be
- Always under attack

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Firewalls _{Keeping} Bad Guys Out



- But a real firewall has to let *something* in or out
- Every castle must have one door

• Otherwise there's no point

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What Really *Is* a Hacker?



- Most people only see superficial details
- A hacker wants to understand the Matrix
- Not necessarily malicious

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Play clip 2 from the movie *Hackers*, typical 90s stereotype (3:57)



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Web Sites Hackers System Crackers Security Experts Cryptologists

System Crackers are Malicious Hackers The Internet Ninjas



- Powers of invisibility
- Like to wear black
- Strike without warning
- Leave no trace
- Make most people uncomfortable

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Web Sites Hackers System Crackers Security Experts Cryptologists

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White Hat Hackers

• Play clip 2, news on White Hat Hackers (2:33)

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Security Experts Internet Jedi



- No effective law enforcement on Internet, like Wild West
- No regulation of software industry
- Nobody to protect people from vendors and crackers

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There Are Temptations



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Cryptologists Modern Wizards



- Start off very weak
- Require many years to develop their powers
- Pore over dusty tomes to find the information they need
- Books are incomprehensible to others
- Full of weird symbols and obscure incantations

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A Powerful Wizard



- Gandalf the White
- Most powerful wizard in Gondor

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Web Sites Cryptology Shift Ciphers Substitution Ciphers Security Experts Advanced Material Cryptologists

Coincidence? I think not.



- Gandalf the White
- Most powerful wizard in Gondor



- Whitfield Diffie
- Chief Security Officer at Sun Microsystems

Cryptology Shift Ciphers Substitution Ciphers Advanced Material Web Sites Hackers System Crackers Security Experts Cryptologists

Have You Ever Wished?



- ...you could walk through walls?
- How about firewalls?
- ...you had one of those invisibility cloaks?
- How about remaining undetected on the Internet?
- ...you could tame monsters?

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- How about remaining undetected on the Internet?
- ...you could tame monsters?

Cryptology Shift Ciphers Substitution Ciphers Advanced Material Web Sites Hackers System Crackers Security Experts Cryptologists

Have You Ever Wished?



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Cryptology Shift Ciphers Substitution Ciphers Advanced Material Web Sites Hackers System Crackers Security Experts Cryptologists

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What All the Words Mean Encryption Machines



- Play clip 4 "A Brief History of Cryptography" (6:11)
- Covers what cryptography is

What All the Words Mean Encryption Machines

What All the Words Mean Encryption Machines

Roman Times

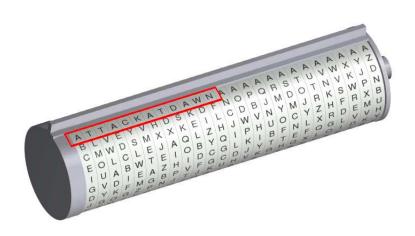


Travis H. Math Rules Cyberspace

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What All the Words Mean Encryption Machines

Jefferson Cylinder - 1790



What All the Words Mean Encryption Machines

WWII - Enigma



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What All the Words Mean Encryption Machines

Korean War



Travis H. Math Rules Cyberspace

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What All the Words Mean Encryption Machines

Late 20th Century Russian Fialka Machine



Travis H. Math Rules Cyberspace

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What All the Words Mean Encryption Machines

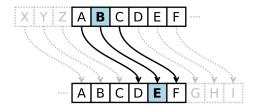
Modern Encryption Machines Almost Everything on the Internet



• If you see these icons, your computer is doing encryption

Explanation Caesar Cipher Example How Is This Math? Cryptanalysis of Shift Cipher Improving the Cipher





Replace input (B) with letter three to the right (E) The number three is called the *key* to the cipher Wraps around To decrypt we do the reverse *ANT* becomes *DQW*

Explanation Caesar Cipher Example How Is This Math? Cryptanalysis of Shift Cipher Improving the Cipher

Caesar Cipher Example

substitution table plaintext ABCDEFGHIJKLMNOPQRSTUVWXYZ ciphertext DEFGHIJKLMNOPQRSTUVWXYZABC

exa	m	р	е

plaintext	THE	QUICK	BROWN	FOX	JUMPS	OVER	THE	LAZY	DOG
ciphertext	WKH	TXLFN	EURZQ	IRA	MXPSV	RYHU	WKH	ODCB	GRJ

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Explanation Caesar Cipher Example How Is This Math? Cryptanalysis of Shift Cipher Improving the Cipher

Hand-On Caesar Cipher

- Write message, encrypt using handout (Vigenère square)
- Plaintext letter is row, move over to the D column; write out letter there
- Swap with your neighbor
- Look up his ciphertext in D column; write out letter at beginning of row

example									
plaintext	THE	QUICK	BROWN	FOX	JUMPS	OVER	THE	LAZY	DOG
ciphertext	WKH	TXLFN	EURZQ	IRA	MXPSV	RYHU	WKH	ODCB	GRJ

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Explanation Caesar Cipher Example How Is This Math? Cryptanalysis of Shift Cipher Improving the Cipher

Changing Symbols

- We use 26 symbols (A-Z); this is called our *alphabet*.
- It's irrelevant to cryptographers.
- For example, we could change to numbers:

A	В	С	D	Е	F	G	H	Ι	J	K	L	M
00	01	02	03	04	05	06	07	08	09	10	11	12
N	0	Р	Q	R	S	Т	U	V	W	X	Y	Z
13	14	15	16	17	18	19	20	21	22	23	24	25

• These are called *ordinal numbers*.

Explanation Caesar Cipher Example How Is This Math? Cryptanalysis of Shift Cipher Improving the Cipher

Encrypting Using Numbers

- Replace A with 0, B with 1, C with 2, ... Z with 25
 Add the key (3) to each number
 - Replace 0 with A, 1 with B, 2 with C, ... 25 with Z
- But wait, what if we went over 25?
 - In that case we subtract 26 from the result
 - So 24 plus 3 is 27, but that's too high, so 27 26 = 1
 - This is called *modular addition*.
 - For decryption, we subtract the key k
 - If we go under zero, then we add 26

Explanation Caesar Cipher Example How Is This Math? Cryptanalysis of Shift Cipher Improving the Cipher

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Explanation Caesar Cipher Example How Is This Math? Cryptanalysis of Shift Cipher Improving the Cipher

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< D > < A >

Explanation Caesar Cipher Example How Is This Math? Cryptanalysis of Shift Cipher Improving the Cipher

How Is This Math?

If x is the plaintext and y is the ciphertext, the equation we're using is:

 $y = (x + 3) \mod 26$

Or more generally, for a key k and an alphabet of n symbols:

 $y = (x + k) \mod n$

Decryption is similar:

$$x = (y - k) \mod n$$

Explanation Caesar Cipher Example How Is This Math? Cryptanalysis of Shift Cipher Improving the Cipher

Shift Ciphers

- The amount we shift is the key
- In Caesar's cipher, the key was 3
- Q: Why do you suppose he chose 3?
- Q: How many keys are there?
- Cryptographers call all of these "Caesar ciphers"

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Explanation Caesar Cipher Example How Is This Math? Cryptanalysis of Shift Cipher Improving the Cipher

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Explanation Caesar Cipher Example How Is This Math? Cryptanalysis of Shift Cipher Improving the Cipher

About the Vigenère Square

- Q: Now that you know the math, what is the Vigenère square doing?
- Q: What do you notice about the square?
- Q: How else could you do the same thing with this square?
- Q: What other tools could help you do the same thing?

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Explanation Caesar Cipher Example How Is This Math? Cryptanalysis of Shift Cipher Improving the Cipher

Other Shift-Cipher Tools



• Were still used in the US Civil War

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Explanation Caesar Cipher Example How Is This Math? Cryptanalysis of Shift Cipher Improving the Cipher

Cryptanalysis of Shift Cipher

encrypted message

Nwcz akwzm ivl amdmv gmiza iow wcz nibpmza jzwcopb nwzbp wv bpqa kwvbqvmvb, i vme vibqwv, kwvkmqdml qv tqjmzbg, ivl Imlqkibml bw bpm xzwxwaqbqwv bpib itt umv izm kzmibml mycit.

• Q: How can we read such a message without knowing the key?

Explanation Caesar Cipher Example How Is This Math? Cryptanalysis of Shift Cipher Improving the Cipher

Trivial Cryptanalysis

encrypted message

Nwcz akwzm ivl amdmv gmiza iow wcz nibpmza jzwcopb nwzbp wv bpqa kwvbqvmvb, i vme vibqwv, kwvkmqdml qv tqjmzbg, ivl Imlqkibml bw bpm xzwxwaqbqwv bpib itt umv izm kzmibml mycit.

- If we know the input is English, there's only a few one-letter words.
- Since the rest of the input is gibberish, and it's not capitalized, "i" must be ciphertext for a.

A D > A A P >

Explanation Caesar Cipher Example How Is This Math? Cryptanalysis of Shift Cipher Improving the Cipher

Classical Countermeasures

- Use all one case (lower or upper)
- Remove punctuation and spaces
- You'll sometimes see them in five-letter groups; that's easier to read and was normal for telegraphs
- But I'm lazy and didn't do that in this talk
- Q: Why doesn't modern cryptography do this?

Explanation Caesar Cipher Example How Is This Math? Cryptanalysis of Shift Cipher Improving the Cipher

Brute Force Attack

encrypted message

nwczakwzmivlamdmvgmizaiowwcznibpmzajzwcopbnwzbpwv bpqakwvbqvmvbivmevibqwvkwvkmqdmlqvtqjmzbgivllmlqki bmlbwbpmxzwxwaqbqwvbpibittumvizmkzmibmlmycit

- Brute force attack tries all 26 possible keys (k=0...25)
- One of them will yield a readable message
- Rest will still look encrypted
- Q: How can you use your handout to do this?

Explanation Caesar Cipher Example How Is This Math? **Cryptanalysis of Shift Cipher** Improving the Cipher

Bruce Force Hands-On

encrypted message

exxegoexsrgi

- Take the day of the month you were born on
- Count over that many columns (use column B if you were born on first of month, etc.)
- Look up this text in that column, write it out

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Explanation Caesar Cipher Example How Is This Math? Cryptanalysis of Shift Cipher Improving the Cipher

Frequency Analysis

- We know that e is the most common letter in English
- Count which is the most common letter in the message
- That's probably the letter e in the original

A D > A A P >

Explanation Caesar Cipher Example How Is This Math? Cryptanalysis of Shift Cipher Improving the Cipher

Frequency Analysis Example

• There's 18 occurences of the letter *m*

encrypted message

nwczakwz**m**ivla**m**dmvgmizaiowwcznibpmzajzwcopbnwzbpwv bpqakwvbqvmvbivmevibqwvkwvkmqdmlqvtqjmzbgivllmlqki bmlbw bpmxzwxwaqbqwvbpibittumvizmkzmibmlmycit

Let
$$y = ord(m) = 12$$
, $x = ord(e) = 4$, and remember:

$$x = (y - k) \mod n$$

$$4 = (12 - k)$$

$$k = (12 - 4) = 8$$

Explanation Caesar Cipher Example How Is This Math? Cryptanalysis of Shift Cipher Improving the Cipher

Frequency Analysis Solution

encrypted message

nwczakwzmivlamdmvgmizaiowwcznibpmzajzwcopbnwzbpwv bpqakwvbqvmvbivmevibqwvkwvkmqdmlqvTqjmzbgivllmlqki bmlbwbpmxzwxwaqbqwvbpibittumvizmkzmibmlmycit

decrypted message (spaces and punctuation added)

Four score and seven years ago our fathers brought forth on this continent, a new nation, conceived in Liberty, and dedicated to the proposition that all men are created equal.

Explanation Caesar Cipher Example How Is This Math? Cryptanalysis of Shift Cipher Improving the Cipher

How Do We Improve the Cipher?

• How do we improve this cipher?

- First, we need to identify the problems.
- Q: What was the problem making brute force possible?
- Q: What was the problem making frequency analysis possible?

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Explanation Caesar Cipher Example How Is This Math? Cryptanalysis of Shift Cipher Improving the Cipher

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Explanation Caesar Cipher Example How Is This Math? Cryptanalysis of Shift Cipher Improving the Cipher

Shift Cipher Review

substitution table

plaintext ABCDEFGHIJKLMNOPQRSTUVWXYZ

ciphertext | DEFGHIJKLMNOPQRSTUVWXYZABC

- Note that the ciphertext alphabet is just the plaintext alphabet slid over
- All we need is one input and one output to figure out the *key* (the amount of the rotation)
- Q: Does multiple encryption fix the problem?

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Explanation Caesar Cipher Example How Is This Math? Cryptanalysis of Shift Cipher Improving the Cipher

Function Composition

 $f(x) = x + 3 \pmod{26}$ $g(x) = x + 4 \pmod{26}$ $h(x) \equiv g(f(x))$ $h \equiv g \circ f$

 $h(x) = (x+3) + 4 \pmod{26}$

• Q: What if f had a key of 17, and g had a key of 14 - what would the key of h be?

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Math Basis Does This Solve Our Problem? Cryptanalysis Transposition, Polyalphabetic

Substitution Cipher

- A *substitution cipher* maps from one alphabet to another
- Can map from and to same alphabet, but scrambled

substitution table

plaintext	ABCDEFGHIJKLMNOPQRSTUVWXYZ
ciphertext	THEQUICKBROWNFXJMPDVRLAZYG

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Memorizing Substitution Ciphers

- Need all 26 ciphertext letters in the right order to encrypt or decrypt.
- Various tricks to remember them, such as using a phrase, eliminating any repetitions, and finishing up alphabet.

substitution table

plaintext	ABCDEFGHIJKLMNOPQRSTUVWXYZ
ciphertext	THEQUICKBROWNFXJMPDVRLAZYG

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Math Basis Does This Solve Our Problem? Cryptanalysis Transposition, Polyalphabetic





- With a partial function,
- some plaintext letters (elements of domain X) don't have known ciphertext letters (elements of co-domain Y)
- This isn't usually the case, and isn't the case here.

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- In our case, every input symbol has an output symbol
- This is called a total function, or usually just a function

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- Every input (in X) has at most one output (in Y)
- This makes it an injective function, or one-to-one

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- Every output (in Y) has at least one input (in X)
- This makes it a *surjective function*, or *onto*

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- A function that is both is known as *bijective*, or *one-to-one* correspondence
- This means that every output has exactly one input

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- A total bijective function whose outputs (codomain) are from the same set as its inputs (domain) is a *permutation*
- Basically, a permutation is just a scrambling of the elements

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In Other Words

classical cryptographer	computer scientist	mathematician
plaintext	input	domain
ciphertext	output	codomain
letter	symbol	element
alphabet	alphabet	set

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Does This Solve Our Problem?

- Caesar cipher had only 26 possible keys
- Q: How many does a substitution cipher have?

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How Many Ways to Scramble 26 Letters?

- First letter may map to any of the 26 letters
- Second letter may map to 25 remaining letters
- Third letter may map to any of 24 remaining
- Do you see a pattern?

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It's a Factorial!

$26 \star (25 \star (24...)) = 26!$

26! = 403291461126605635584000000

You've now discovered how to find out how many permutations are possible for a set. For n elements, it's n factorial! This is far too many to try them all (brute force)

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Sample Substitution

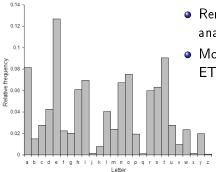
encrypted message

LIVITCSWPIYVEWHEVSRIQMXLEYVEOIEWHRXEXIPFEMVEWHKVSTYLXZIXLIKIIXPIJVSZEYPER RGERIMWQLMGLMXQERIWGPSRIHMXQEREKIETXMJTPRGEVEKEITREWHEXXLEXXMZITWAWSQWXSW EXTVEPMRXRSJGSTVRIEYVIEXCVMUIMWERGMIWXMJMGCSMWXSJOMIQXLIVIQIVIXQSVSTWHKPE GARCSXRWIEVSWIIBXVIZMXFSJXLIKEGAEWHEPSWYSWIWIEVXLISXLIVXLIRGEPIRQIVIIBGII HMWYPFLEVHEWHYPSRRFQMXLEPPXLIECCIEVEWGISJKTVWMRLIHYSPHXLIQIMYLXSJXLIMWRIG XQEROIVFVIZEVAEKPIEWHXEAMWYEPPXLMWYRMWXSGSWRMHIVEXMSWMGSTPHLEVHPFKPEZINTC MXIVJSVLMRSCMWMSWVIRCIGXMWYMX

- So how would you *cryptanalyze* this?
- Taking the spaces out is a common trick and usually doesn't hurt readability of plaintext

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English Letter Frequency Distribution



- Remember frequency analysis?
- Most common letters are: ETAOINSHRDLCU...

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- *bigrams* are pairs of letters
- most common is "th", followed by "he", and others

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- *trigrams* are three letters in a row
- most common is "the", followed by "and", "tha", etc.

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Attacking It 1

encrypted message

LIVITCSWPIYVEWHEVSRIQMXLEYVEOIEWHRXEXIPFEMVEWHKVSTYLXZIXLIKIIXPIJVSZEYPER RGERIMWQLMGLMXQERIWGPSRIHMXQEREKIETXMJTPRGEVEKEITREWHEXXLEXXMZITWAWSQWXSW EXTVEPMRXRSJGSTVRIEYVIEXCVMUIMWERGMIWXMJMGCSMWXSJOMIQXLIVIQIVIXQSVSTWHKPE GARCSXRWIEVSWIIBXVIZMXFSJXLIKEGAEWHEPSWYSWIWIEVXLISXLIVXLIRGEPIRQIVIIBGII HMWYPFLEVHEWHYPSRRFQMXLEPPXLIECCIEVEWGISJKTVWMRLIHYSPHXLIQIMYLXSJXLIMWRIG XQEROIVFVIZEVAEKPIEWHXEAMWYEPPXLMWYRMWXSGSWRMHIVEXMSWMGSTPHLEVHPFKPEZINTC MXIVJSVLMRSCMWMSWVIRCIGXMWYMX

- I was most common letter, XL most common bigram, XLI most common trigram
- Guessed that XLI=the

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Attacking It 2

encrypted message

heVeTCSWPeYVaWHaVSReQMthaYVaOeaWHRtatePFaMVaWHKVSTYhtZetheKeetPeJVSZaYPaR RGaReMWQhMGhMtQaReWGPSReHMtQaRaKeaTtMJTPRGaVaKaeTRaWHatthattMZeTWAWSQWtSW atTVaPMRtRSJGSTVReaYVeatCVMUeMWaRGMeWtMJMGCSMWtSJOMeQtheVeQeVetQSVSTWHKPa GARCStRWeaVSWeeBtVeZMtFSJtheKaGAaWHaPSWYSWeWeaVtheStheVtheRGaPeRQeVeeBGee HMWYPFhaVHaWHYPSRRFQMthaPPtheaCCeaVaWGeSJKTVWMRheHYSPHtheQeMYhtSJtheMWReG tQaROeVFVeZaVAaKPeaWHtaAMWYaPPthMWYRMWtSGSWRMHeVatMSWMGSTPHhaVHPFKPaZeNTC MteVJSVhMRSCMWMSWVeRCeGtMWYMt

- heVe = here, Rtate = state, atthattMZe = atthattime
- means V=r, R=s, M=i, Z=m

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Attacking It 3

encrypted message

 $\label{eq:hererCSWPeYraWHarSseQithaYraOeaWHstatePFairaWHKrSTYhtmetheKeetPeJrSmaYPassaseiWQhiGhitQaseWGPSseHitQasaKeaTtiJTPsGaraKaeTsaWHatthattimeTWAWSQWtSWatTraPistsSJGSTrseaYreatCriUeiWasGieWtiJiGCSiWtSJOieQthereQeretQSrSTWHKPaGAsCStsWearSWeeBtremitFSJtheKaGAaWHaPSWYSWeWeartheStherthesGaPesQereeBGeeHiWYPFharHaWHYPSssFQithaPPtheaCCearaWGeSJKTrWisheHYSPHtheQeiYhtSJtheiWseGtQasOerFremarAaKPeaWHtaAiWYaPPthiWYsiWtSGSWsiHeratiSWiGSTPHharHPFKPameNTCiterJSrhisSCiWiSWresCeGtiWYit$

remarA = remark, and so on...

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Done

decrypted message

hereuponlegrandarosewithagraveandstatelyairandbroughtmethebeetlefromaglas scaseinwhichitwasencloseditwasabeautifulscarabaeusandatthattimeunknownton aturalistsofcourseagreatprizeinascientificpointofviewthereweretworoundbla ckspotsnearoneextremityofthebackandalongoneneartheotherthescaleswereexcee dinglyhardandglossywithalltheappearanceofburnishedgoldtheweightoftheinsec twasveryremarkableandtakingallthingsintoconsiderationicouldhardlyblamejup iterforhisopinionrespectingit

• Add spaces between words, and...

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Adding Spaces

decrypted message

Hereupon Legrand arose, with a grave and stately air, and brought me the beetle from a glass case in which it was enclosed. It was a beautiful scarabaeus, and, at that time, unknown to naturalists-of course a great prize in a scientific point of view. There were two round black spots near one extremity of the back, and a long one near the other. The scales were exceedingly hard and glossy, with all the appearance of burnished gold. The weight of the insect was very remarkable, and, taking all things into consideration, I could hardly blame Jupiter for his opinion respecting it.

- Abracadbra, we're done.
- How do we solve this? Well...

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• Play clip 5, video which talks about transposition ciphers (9:59)



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Polyalphabetic Substitution Ciphers

- Play clip 6 (20:28), skip to 15:34 for Vigenère cipher (4:56 net)
- Covers polyalphabetic substitution ciphers

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Polyalphabetic Cipher Hands-On

plaintext	ATTACKATDAWN
key	LEMONLEMONLE

You should get LXFOPVEFRNHR

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Polyalphabetic Cipher Hands-On

plaintext	ATTACKATDAWN
key	LEMONLEMONLE

You should get LXFOPVEFRNHR

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Breaking Substitution Ciphers

- Breaking these is an advanced topic
- It's called Kasiski Examination
- But you have half the knowledge already
- Q: Would multiple encryption help?

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Functional Composition

- If the f(x) mapped A to G, and B to X
- And g(x) mapped G to Y, and X to C
- You could just have h(x) map A to Y and B to C

Manhattan Project Cipher Steganography (opt) Playfair (opt) One-Time Pad (opt) Enigma (opt)

The Manhattan Project Cipher

- Pick out an 11x11 grid on your graph paper
- Number them 0..9 along X and Y axes; this gives you a 10x10 grid (this is 100 squares)
- Fill all 100 squares with this many of each letter (eight As, one B, etc.):
- A 8, B 1, C 3, D 4, E 13, F 2, G 2, H 6, I 7, J 1, K 1, L 4, M
 2, N 6, O 7, P 2, Q 1, R 6, S 6, T 9, U 2, V 1, W 2, X 1, Y 2, Z 1
- Encrypt by picking a letter at random, then writing down the X, Y coordinates (commas are not necessary)

Manhattan Project Cipher Steganography (opt) Playfair (opt) One-Time Pad (opt) Enigma (opt)



- Play clip S to explain steganography (2:30)
- Steganography is not cryptography, but similar in some ways

Manhattan Project Cipher Steganography (opt) Playfair (opt) One-Time Pad (opt) Enigma (opt)



• Play clip P which rapidly covers playfair cipher (3:00)

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Manhattan Project Cipher Steganography (opt) Playfair (opt) **One-Time Pad (opt)** Enigma (opt)

One-Time Pad (OTP)

- Play OTP video 1 explaining OTPs (2:42)
- Play OTP video 2 recording of a numbers station (1:56)
- Q: Notice anything about the groupings of numbers?

Manhattan Project Cipher Steganography (opt) Playfair (opt) One-Time Pad (opt) Enigma (opt)

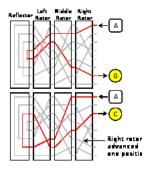




- Play clip E1 "The Enigma Machine" (3:39)
- Talk about how rotors act as substitution ciphers
- Play clip E2 video "My Enigma" (3:44)

Computer SecurityManhattan Project CipherCryptologySteganography (opt)Shift CiphersPlayfair (opt)Substitution CiphersOne-Time Pad (opt)Advanced MaterialEnigma (opt)

Rotor Assembly



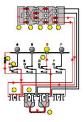
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Manhattan Project Cipher Steganography (opt) Playfair (opt) One-Time Pad (opt) Enigma (opt)

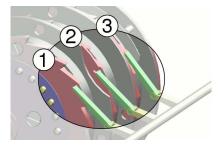




- Red shows electrical current
- Battery (1) to key A (2) to plugboard (3) to fixed entry wheel
 (4) through rotors (5), to reflector (6)
- back through rotors (5 and 4), to plug S (7) through cable to D (8) and lighting up light D (9)

Manhattan Project Cipher Steganography (opt) Playfair (opt) One-Time Pad (opt) Enigma (opt)

But That's Not All



- With each keypress, the wheels rotated
- rotors 1-2-3 advance like seconds-minutes-hours on a clock

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 Computer Security
 Manhattan Project Cipher

 Cryptology
 Steganography (opt)

 Shift Ciphers
 Playfair (opt)

 Substitution Ciphers
 One-Time Pad (opt)

 Advanced Material
 Enigma (opt)

This Is Math Too

$E = PRMLUL^{-1}M^{-1}R^{-1}P^{-1}$

 Where E is encryption function, P is plugboard, R/M/L right/middle/left rotors, U is reflector

 $E = P(r^{i}Rr^{-i})(r^{j}Mr^{-j})(r^{k}Lr^{-k})U(r^{k}L^{-1}r^{-k})(r^{j}M^{-1}r^{-j})(r^{i}R^{-1}r^{-i})P^{-1}$

- r is the cyclic permutation operator
- Don't feel bad if you don't understand this

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 Computer Security
 Manhattan Project Ciphe Cryptology

 Shift Ciphers
 Playfair (opt)

 Substitution Ciphers
 One-Time Pad (opt)

 Advanced Material
 Enigma (opt)

Further Reading

- Keep your handout, it has a link to the extra material and my email address
- Take 5 minutes to fill out your survey
- If this is your last class, please give me your survey packets to turn in

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